



**De:** crm@crm.umontreal.ca  
**Objet:** COLLOQUE DES SCIENCES MATHÉMATIQUES DU QUÉBEC (26/03/2015, Steve Boyer)  
**Date:** 23 mars 2015 09:55  
**À:** activites@CRM.UMontreal.CA

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Le café sera servi à 15h30 / BURN 1024 /  
Coffee will be served at 3:30 pm / BURN 1024.

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COLLOQUE DES SCIENCES MATHÉMATIQUES DU QUÉBEC - Montréal  
<http://www.crm.umontreal.ca/Colloques/colloqueSMQ-Montreal.html>  
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DATE :  
Le jeudi 26 mars 2015 / Thursday, March 26, 2015

HEURE / TIME :  
16 h / 4:00 p.m.

CONFERENCIER(S) / SPEAKER(S) :  
Steve Boyer (UQAM)

TITRE / TITLE :  
Left-orderings of groups and the topology of 3-manifolds

LIEU / PLACE :  
McGill University, Burnside Hall, 805 rue Sherbrooke O., Montréal, salle 920

RESUME / ABSTRACT :  
Many decades of work culminating in Perelman's proof of Thurston's geometrisation conjecture showed that a closed, connected, orientable, prime 3-dimensional manifold  $M$  is essentially determined by its fundamental group  $\pi_1(M)$ . This group consists of classes of based loops in  $M$  and its multiplication corresponds to their concatenation. An important problem is to describe the topological and geometric properties of  $M$  in terms of  $\pi_1(M)$ . For instance, geometrisation implies that  $M$  admits a hyperbolic structure if and only if  $\pi_1(M)$  is infinite, freely indecomposable, and contains no  $\mathbb{Z} \oplus \mathbb{Z}$  subgroups. In this talk I will describe recent work which has determined a surprisingly strong correlation between the existence of a left-order on  $\pi_1(M)$  (a total order invariant under left multiplication) and the following two measures of largeness for  $M$ :

- a) the existence of a co-oriented taut foliation on  $M$  - a special type of partition of  $M$  into surfaces which fit together locally like a deck of cards.
- b) the condition that  $M$  not be an L-space - an analytically defined condition representing the non-triviality of its Heegaard-Floer homology.

I will introduce each of these notions, describe the results which connect them, and state a number of open problems and conjectures concerning their precise relationship.