# Nonlinear Continuous Deformation of an Image Based on a Set of Intersecting Straight Lines 

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## Team common language

French

## References

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3. Z. Zhang, A Flexible New Technique for Camera Calibration, Technical Report MSR-TR-98-71, Microsoft Research, 1998.
4. O. Faugeras, Three-Dimensional Computer Vision, MIT Press, 1993 (Chapter 2).


#### Abstract

Let $I$ be a closed area within the plane, i.e., an image, which can be assumed to be a rectangle. Let $D_{i}$ be a set of equidistant points belonging to a straight line and included in $I$. Let $A=\left\{D_{i} \mid i=1,2, \ldots, M\right\}$ be a collection of $M$ straight lines. Some of the intersection points of lines in $A$ may belong to $I$. Finally, let $g(x, y)$ be a function from the plane into itself representing a nonlinear, continuous and smooth deformation of $I$. Given $g(A)$, i.e., the image under $g$ of the union of all the $D_{i}$, the problem is to find a method for estimating $g$.

The function $g$ to be estimated represents the nonlinear image deformation produced by the lens of a camera. There are several simple models of this deformation (see references nos. 3 and 4 above). We are looking, however, for a solution independent of the lens type, although certain assumptions may be made. In general, the points belonging to a given straight line will be neither colinear, nor equidistant, after having been "transformed" by $g$. One may retain the assumption that the points belonging to a straight line $D_{i}$ will belong to a convex segment after their transformation. One may also assume that $g$ is radially symmetric with respect to a point that is not known a priori. Note that the original coordinates of the points are unknown; only the incidence relation between points and lines is known.

The difficulty lies in trying to control the behaviour of the function $g$ near the points where two lines $D_{i}$ and $D_{j}$ intersect, or, more precisely, near a pair of points close to one another but that do not belong to the same


line. The naive approach consists in estimating the deformation separately for each line; this approach can produce a solution that is not consistent near the intersection points. For the same reason, computing the average of the deformations does not yield a valid solution in general. Our suggestion is to define a cost measure, for instance an elastic energy, to constrain the function $g$.

