Workshop on Singularities, Hamiltonian and gradient flows Atelier sur les singularités, flots hamiltoniens et gradients 12–16 May/Mai, 2008

A Monotonicity Formula Approach for Higher Dimensional Hyperbolic PDE

Markus KEEL

Department of Mathematics University of Minnesota 127 Vincent Hall, 206 Church St. S.E. Minnneapolis, MN 55455 USA

keel@math.umn.edu

Abstract

We will discuss joint work with Philippe Lefloch and Terry Tao. The aim of the work is to understand a family of already established estimates ("null form estimates") for the linear wave equation from the point of view of a monotonicity formula. We will describe such a proof for one family of null form estimates in higher dimensions $(n \ge 7)$. The result is analogous to previously established "interaction estimates" for Schrödinger equations when n = 3 and certain hyperbolic equations when n = 1.