

Workshop on Interactions Between  
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## General LLT polynomials

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### Abstract

I'll report on *joint work with Grojnowski* in which we give a general definition of LLT polynomials associated to a reductive algebraic group  $G$  and Levi subgroup  $L$ , and prove that their coefficients are always positive. The case  $G = \mathrm{GL}_n$  gives the classical LLT polynomials, including those for skew shapes, whose positivity was an open problem. The proof uses the geometric machinery of Kazhdan-Lusztig theory.