

# The extended degree zero subalgebra of the Ext algebra of a linear module

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Let  $\mathbb{k}$  be a field and let  $R$  be a Koszul  $\mathbb{k}$ -algebra. Let  $M$  be a linear  $\mathbb{k}$ -module and let  $\Gamma$  be the Ext-algebra of  $M$ . View  $\Gamma$  as a bigraded algebra with the bigrading induced by the homological degree and by the internal grading of  $M$ , that is

$$\Gamma = \text{Ext}_R^*(M, M) = \bigoplus_{n \geq 0} \bigoplus_{i \in \mathbb{Z}} \text{Ext}_R^n(M, M)_i.$$

We consider next *the extended degree zero subalgebra*  $\Delta_M$  of  $\Gamma$ ,

$$\Delta_M = \bigoplus_{n \geq 0} \text{Ext}_R^n(M, M)_0.$$

So  $\Delta_M$  is generated by all the homogeneous elements of  $\Gamma$  having internal degree zero. It turns out that the extended degree zero subalgebra can be used to obtain a characterization of the graded center of a Koszul algebra. I will also present some other applications of the ideas involved.

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