

# Cluster categories of type $A$ double infinity

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Cluster categories have been introduced about 8 years ago by Buan, Marsh, Reiten, Reineke and Todorov with the hope of understanding some of the combinatorics of the famous cluster algebras. Given any finite acyclic quiver  $Q$ , the cluster category  $C(Q)$  attached to  $Q$  is defined. This is a nice hom-finite 2-Calabi—Yau triangulated category. This construction actually works for any infinite quiver that is locally finite without infinite paths. In this talk, we will consider the cluster category attached to a quiver of type  $A$  double infinity and show that this category has a geometric realization. Indecomposable objects, morphisms, extensions and cluster-tilting subcategories will all be described.

*Joint work with Shiping Liu.*

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