

# Conformally Kähler constant scalar curvature metrics with $J$ -invariant Ricci tensor

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We describe a study of the metrics in the title, also called conformally Kähler, Einstein-Maxwell metrics. A main feature is the existence of an invariant of Futaki type, determined by a Kähler class, a compact group of automorphisms  $G$  with a fixed Killing field in its Lie algebra having a positive Killing potential  $f$ , and a fixed positive constant. Nonvanishing of this invariant obstructs the existence of a  $G$ -invariant Kähler metric  $g$  in the Kähler class such that  $g/f^2$  is Einstein-Maxwell. We will discuss applications of this and related concepts in the toric case.

*This is joint work with V. Apostolov.*

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