

Thermal QCD at finite gauge coupling from string/M theory involving six-/seven-folds of SU(3)-/G₂-structure

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We will discuss the delocalized Strominger-Yau-Zaslow mirror of the McGill type IIB dual of large- N thermal QCD involving N black $D3$ -branes, M $D5$ (and anti- $D5$) branes wrapping a two-cycle and $N_f D7$ (and anti- $D7$) branes embedded via the Ouyang embedding in a non Kaehler resolved warped deformed conifold (NKRWDC), and its M -theoretic uplift to black $M3$ -branes which could be thought of as black $M5$ -branes wrapping a two-cycle in an asymptotic $\text{AdS}_5 \times M_6$. We will do so in a large- N limit referred to as the MQGP limit involving $g_s \ll 1$ [given that sQGP is expected to involve a finite gauge coupling (thereby necessitating addressing the gravity dual from an M -theory perspective)], finite M , large N and small $g_s M^2/N$. In this process, building up on the fact that deviation of three-form fluxes from being ISD is UV and (small) resolution-parameter-suppressed, the following will also be discussed:

- (i) We will see that in the MQGP limit, locally, the $SU(3)$ structure torsion classes follow : $\tau(IIB)_{SU(3)} = W_4 + W_5$ (such that $2/3W_5^{3\text{bar}} = W_4^{3\text{bar}}$ implying KS-like supersymmetry) — Delocalized SYZ mirror $\rightarrow \tau(\text{IIA})_{SU(3)} = W_2 + W_4 + W_5$, i.e., the large- N -suppression of the NKRWDC's deviation from being complex, is lost in taking the mirror. With a further fine tuning, however, the same can approximately be recovered $W_2 \approx 0$;
1. (ii) We will work out a local G_2 structure of the M -theory uplift after a fine tuning of the mirror type IIA metric, and find the G_2 structure torsion classes: $\tau_{G_2} = W_{14} + W_{27}$ in the large- N limit G_2 structure approaches G_2 holonomy;

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- (iii) the local T^3 used for implementing SYZ mirror symmetry as a triple T dual, in the UV, will be shown to satisfy the same conditions as the maximal T^2 -invariant special Lagrangian three-cycles of deformed conifold (if deformation $>$ resolution in the RWDC) and resolved conifold (if resolution $>$ deformation in the RWDC);
- (iv) We will show that with the mass of the lightest vector meson as an input it is possible to obtain the QCD deconfinement temperature T_c consistent with the lattice results with (the number of colors) $N \sim 10$ as well as the correct mass scale of the light (first generation) quarks, at the same time ensuring the thermodynamical stability of the type IIB background;
- (v) Using the $D = 11\text{EH} + \text{GHY} + \text{Flux} + \text{O}(R^4)$ action, we will demonstrate the thermodynamical stability of the local M -theoretic uplift by demonstrating positivity of the specific heat;
- (vi) We will discuss evaluation of a host of two-point functions involving gauge field fluctuations about a baryon chemical potential background (leading to the evaluation of DC electrical conductivity and charge susceptibility) and metric fluctuations (leading to the evaluation of shear viscosity and thus shear viscosity ? entropy density ratio, and speed of sound).