

The first function

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Let $s(n)$ denote the sum of the positive divisors of n that are smaller than n . Introduced by Pythagoras 2500 years ago, it is perhaps the first function ever studied in mathematics. Steeped in numerology and colorful metaphors, the ancient problems associated with $s(n)$ have led to much of number theory, including some very recent results.

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