

# On the counting function of the range of the Carmichael $\lambda$ -function

Florian Luca\*

[fluca@matmor.unam.mx](mailto:fluca@matmor.unam.mx)

---

The Carmichael  $\lambda$ -function associates to  $n$  the exponent  $\lambda(n)$  of the multiplicative group modulo  $n$ . In my talk, I will describe the main ideas behind the proof that the counting function  $\#\{\lambda(n) \leq x\}$  of the range of the Carmichael function  $\lambda(n)$  below  $x$  is  $x/(\log x)^{\eta+o(1)}$  as  $x \rightarrow \infty$ , where  $\eta = 1 - (1 + \log \log 2)/\log 2 = 0.08607 \dots$  is the Erdős–Tenebaum–Ford constant. The proof uses sieve methods.

*This is joint work with Kevin Ford and Carl Pomerance.*

---

\*School of Mathematics, University of the Witwatersrand, Wits 2050, SOUTH AFRICA.