

# Oriented Brauer categories

Jonathan Brundan<sup>\*</sup>

[brundan@darkwing.uoregon.edu](mailto:brundan@darkwing.uoregon.edu)

WEB: [pages.uoregon.edu/brundan/](http://pages.uoregon.edu/brundan/)

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The oriented Brauer category  $\text{OB}$  is the free  $K$ -linear symmetric monoidal category generated by a single object and its dual. I will talk about its representations (= the  $K$ -linear functors from  $\text{OB}$  to vector spaces), which can be understood via a triangular decomposition  $\text{OB} = \text{OB}^- \text{OB}^0 \text{OB}^+$  in which the diagonal part  $\text{OB}^0$  looks roughly like a product of two symmetric groups. There is also an affine analog of the category  $\text{OB}$  obtained by adjoining an extra polynomial generator. The affine oriented Brauer category has various cyclotomic quotients, the simplest of which recovers the original category  $\text{OB}$ . In general these cyclotomic quotients categorify certain tensor products of lowest and highest weight representations.

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<sup>\*</sup>Department of Mathematics, University of Oregon, Eugene, OR 97403, USA.